

$$\lim_{x \rightarrow 0} \left(\frac{1 + \sin(x) * \cos(\alpha * x)}{1 + \sin(x) * \cos(\beta * x)} \right)^{ctg^3 x} =$$

$$\lim_{x \rightarrow 0} \left(1 + \frac{\sin(x) * \cos(\alpha * x) - \sin(x) * \cos(\beta * x)}{1 + \sin(x) * \cos(\beta * x)} \right)^{\frac{\cos^3 x}{\sin^3 x}} =$$

$$\lim_{x \rightarrow 0} \left(1 + \sin(x) * \frac{\cos(\alpha * x) - \cos(\beta * x)}{1 + \sin(x) * \cos(\beta * x)} \right)^{\frac{1}{\sin^3 x}} =$$

$$\lim_{x \rightarrow 0} \left(1 + \sin(x) * \frac{\cos(\alpha * x) - \cos(\beta * x)}{1} \right)^{\frac{1}{\sin^3 x}} =$$

$$\lim_{x \rightarrow 0} \left(1 - 2 \sin(x) * \sin\left(\frac{(\alpha + \beta) * x}{2}\right) \sin\left(\frac{(\alpha - \beta) * x}{2}\right) \right)^{\frac{1}{\sin^3 x}} =$$

$$\lim_{x \rightarrow 0} \left(1 - 2 * \sin(x) * \frac{(\alpha + \beta)}{2} \frac{(\alpha - \beta)}{2} \sin(x) * \sin(x) \right)^{\frac{1}{\sin^3 x}} =$$

$$\lim_{x \rightarrow 0} \left(1 - \sin^3(x) * \frac{(\alpha^2 - \beta^2)}{2} \right)^{\frac{1}{\sin^3 x}} =$$

$$\lim_{x \rightarrow 0} \left(1 - \sin^3(x) * \frac{(\alpha^2 - \beta^2)}{2} \right)^{\left(\frac{1}{-\sin^3 x * \frac{(\alpha^2 - \beta^2)}{2}} \right) * \left(-\frac{(\alpha^2 - \beta^2)}{2} \right)} = e^{\frac{(\alpha^2 - \beta^2)}{2}} = e^{\frac{\alpha^2}{2}} * e^{\frac{\beta^2}{2}}$$