

$$\textcircled{2} \quad I_2 = \int \frac{dx}{1+\cos^2 x} = \left| \begin{array}{l} z = \operatorname{tg} \frac{x}{2} \\ \cos x = \frac{1-z^2}{1+z^2} \\ dx = \frac{2dz}{1+z^2} \end{array} \right| = \int \frac{2dz}{1+\left(\frac{1-z^2}{1+z^2}\right)^2} =$$

$$= 2 \int \frac{dz}{1+z^2 + \frac{(1-z^2)^2}{1+z^2}} = 2 \int \frac{(1+z^2)dz}{(1+z^2)^2 - (1-z^2)^2} = 2 \int \frac{(1+z^2)dz}{1+2z^2+z^4-1+2z^2-z^4} =$$

$$= 2 \int \frac{(1+z^2)dz}{4z^2} = 2 \int \frac{dz}{4z^2} + 2 \int \frac{z^2 dz}{4z^2} =$$

$$= \frac{1}{2} \int \frac{dz}{z^2} + \frac{1}{2} \int dz = -\frac{1}{2} \cdot z^{-1} + \frac{1}{2} z + C_2 =$$

$$= \frac{z}{2} - \frac{1}{2z} + C_2 = \frac{z^2-1}{2z} + C_2 = \left| z = \operatorname{tg} \frac{x}{2} \right| =$$

$$= \frac{\operatorname{tg}^2 \frac{x}{2} - 1}{2 \operatorname{tg} \frac{x}{2}} + C_2$$

$$I = -2 \ln |\cos x| + \ln |\cos^2 x + 1| + 2C_1 + \frac{3 \operatorname{tg}^2 \frac{x}{2} - 1}{2 \operatorname{tg} \frac{x}{2}} + 3C_2 =$$

$$= \ln \left| \frac{\cos^2 x}{\cos x + 1} \right| + \frac{3}{2} \operatorname{tg} \frac{x}{2} - \frac{1}{2} \operatorname{tg} \frac{x}{2} + C_3$$

$$= \ln \left| \frac{1+\cos^2 x}{\cos^2 x} \right| + \frac{3}{2} \left(\operatorname{tg} \frac{x}{2} - \operatorname{ctg} \frac{x}{2} \right) + C_3$$